



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

Methods to estimate the epidemic reproduction number

Anne Cori

a.cor@imperial.ac.uk

MRC Centre for Global Infectious Disease Analysis

*School of Public Health
Imperial College London*

Modelling to Support Resilience for Pandemics
Cambridge
22 June 2022



MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

With apologies in advance for the self sales pitch

The reproduction number R_t



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

R_t = average number of secondary cases infected by each case “at time t”

→ Easy to interpret

→ Useful at different stages of an outbreak, to:

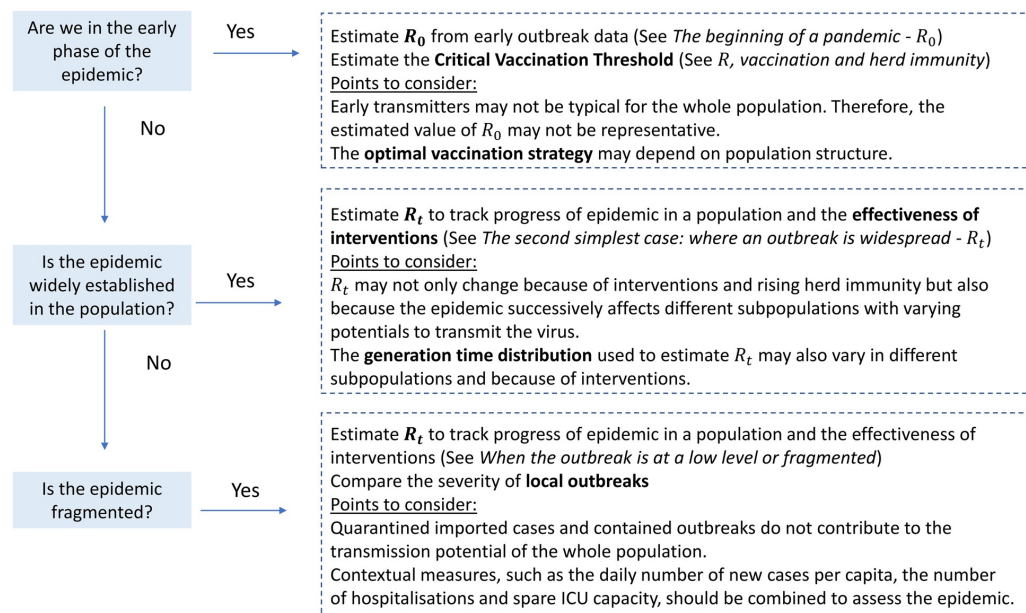
1. **Predict** the potential impact of the outbreak
2. **Assess** the feasibility of control measures
3. **Track** potential changes in transmissibility over time
4. **Evaluate** the effectiveness of control measures

The reproduction number R_t



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London





MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

Why should we care?

Why should we care?



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

-
- **“We know when cases are going up and we are going to be overwhelmed” (HCWs)**
 - **“The growth rate is more informative.” (Many people)**

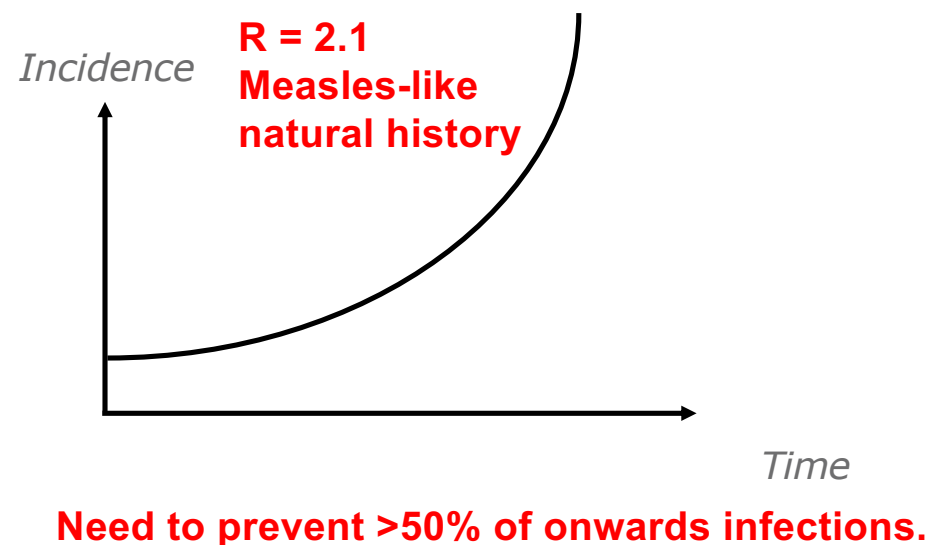
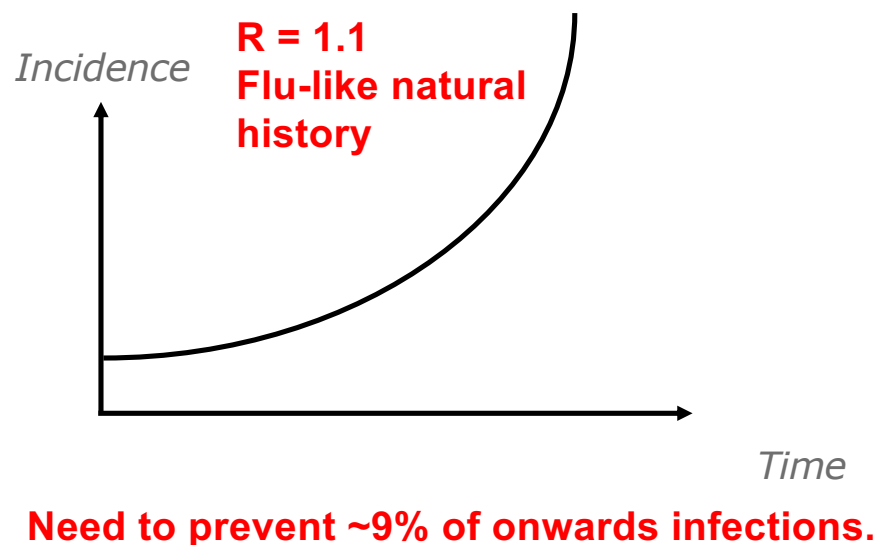
Why should we care?



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

- “We know when cases are going up and we are going to be overwhelmed” (HCWs)
- “The growth rate is more informative.” (Many people)
 - **Yes:** the growth rate tells you how fast cases are growing / declining
 - **No:** the growth rate doesn’t tell you how much effort is needed for control

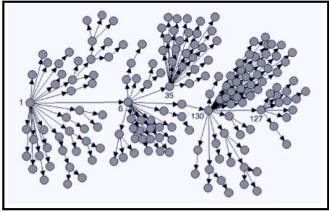


A multitude of approaches



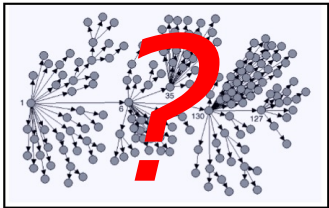
MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London



- **Contact tracing**

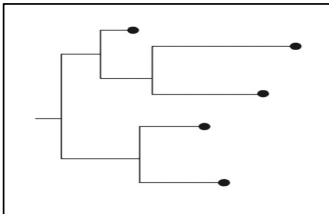
e.g. Tsang et al. NEJM 2003



- **Inferring who infected whom**

Wallinga & Teunis AJE 2004

Jombart et al. PLoS Comp Biol 2014



- **Fitting a model to genetic data**

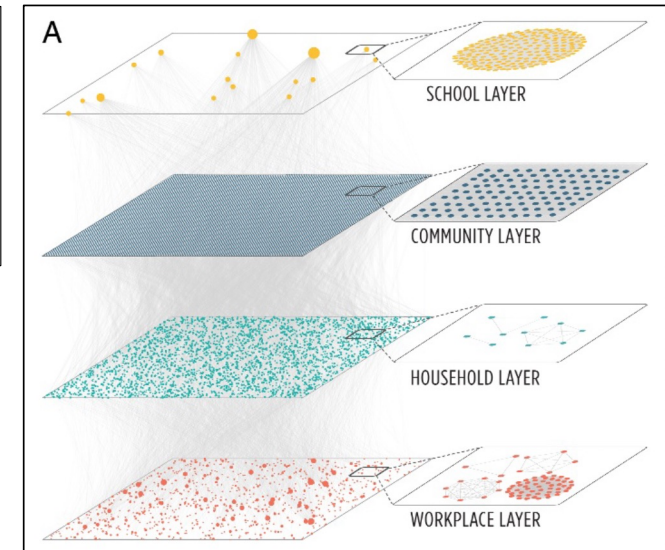
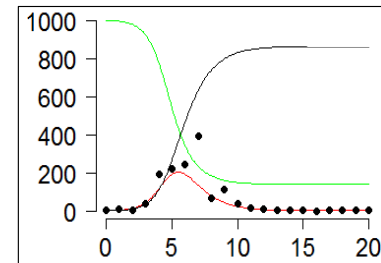
Stadler et al. MBE 2011

Volz & Siveroni PLoS Comp Biol 2018

- **Mechanistic model fitting to epi data**

e.g. Kucharski et al. PNAS 2015,

Liu et al. PNAS 2018



NOT AN EXHAUSTIVE LIST!

Common issues



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

-
- Expensive, not easily scalable
 - Not feasible in real-time (require future data AND/OR too long to develop)
 - Require many assumptions (about the population, the pathogen, etc)

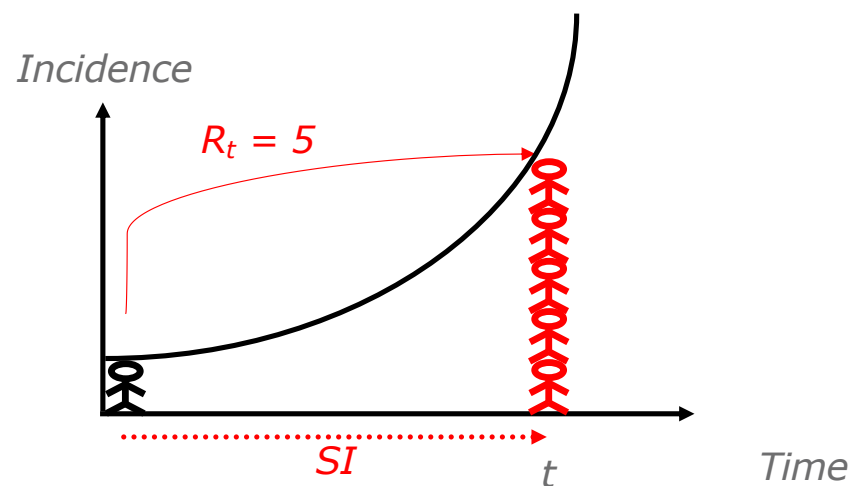
So let's go super simple



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

- R_t can be estimated using data on incidence and the serial interval SI

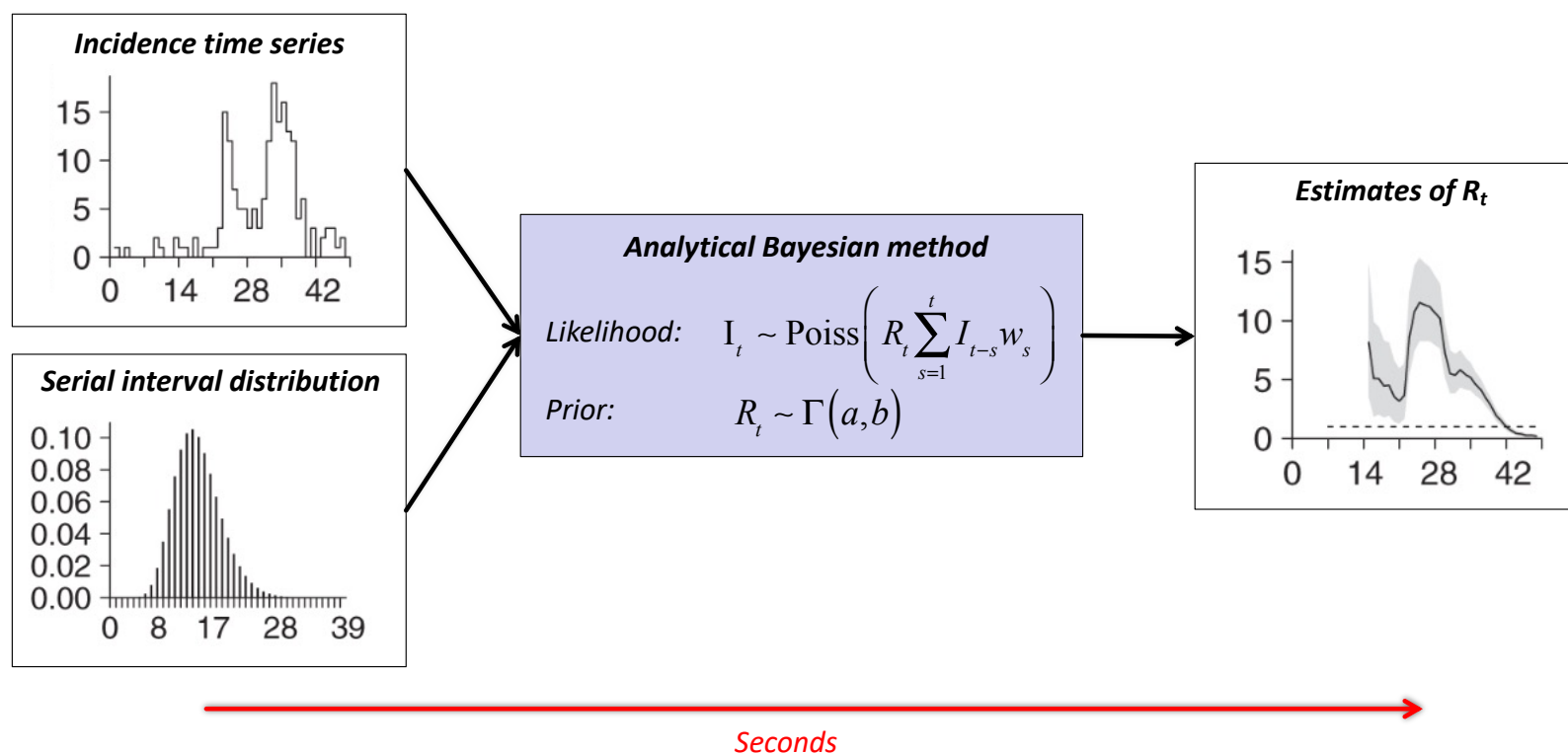


The EpiEstim method



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London



<http://tools.epidemiology.net/EpiEstim.xls>
<http://cran.r-project.org/web/packages/EpiEstim/index.html>
<https://shiny.dide.imperial.ac.uk/epiestim/>

Cori et al. AJE 2013



MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

**“But this is really simple”
(again, many people)**

It's simple but it works well



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

“For near real-time estimation of R_t , we recommend the approach of Cori and colleagues, which uses data from before time t and empirical estimates of the distribution of time between infections.”

And people use it a lot



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

A new framework and software to estimate time-varying reproduction numbers during epidemics

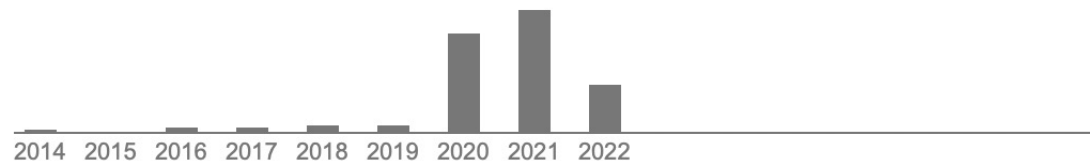
[\[HTML\] from oup.com](#)
[Full View](#)

Authors Anne Cori, Neil M Ferguson, Christophe Fraser, Simon Cauchemez

Publication date 2013/11/1

Journal American journal of epidemiology

Total citations [Cited by 1063](#)



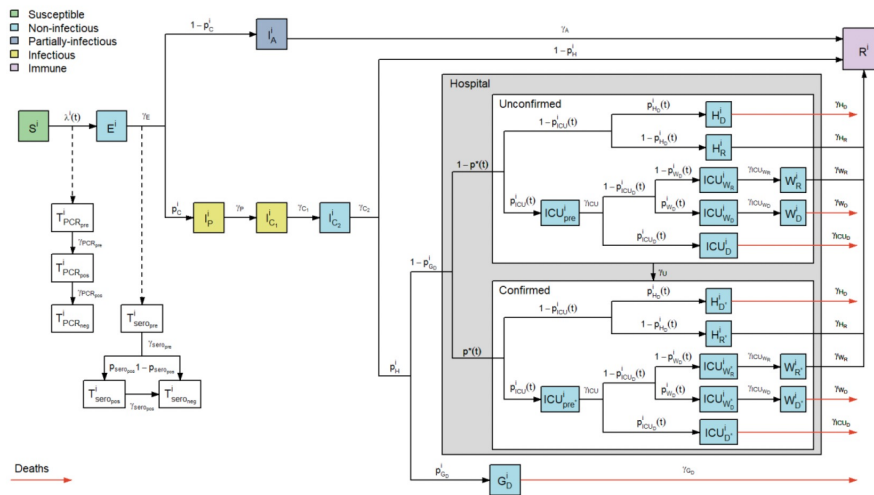


MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

Is it too simple?

It gives similar estimates to more complex models



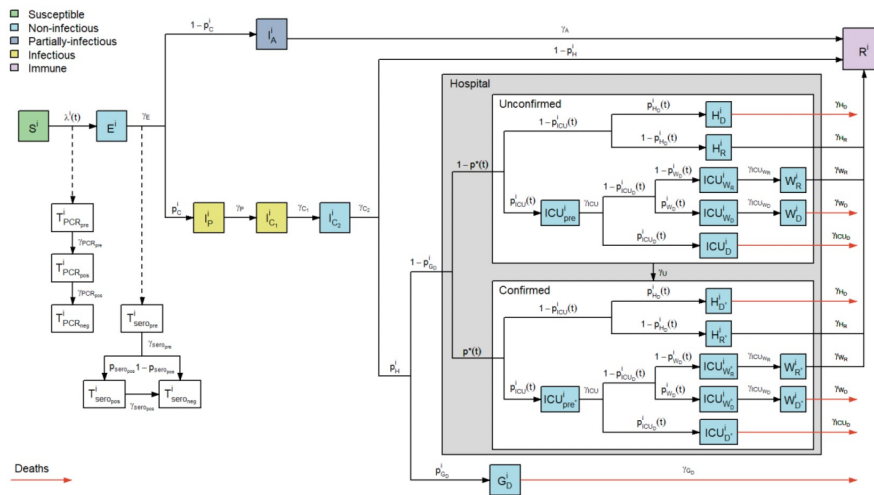
(722 compartments)

It gives similar estimates to more complex models

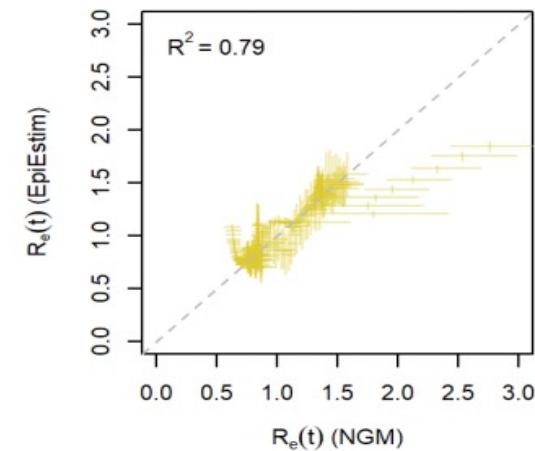
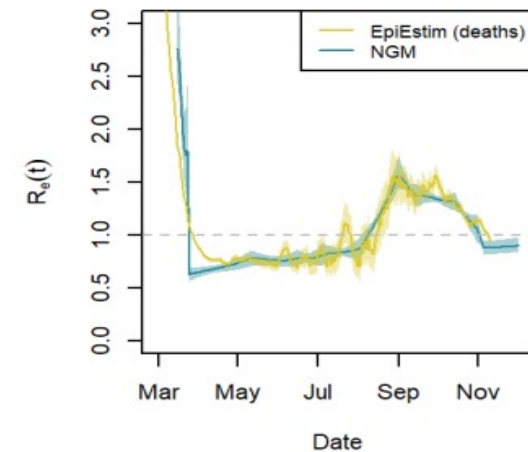


MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London



(722 compartments)



Knock et al. Science Translational Medicine 2021

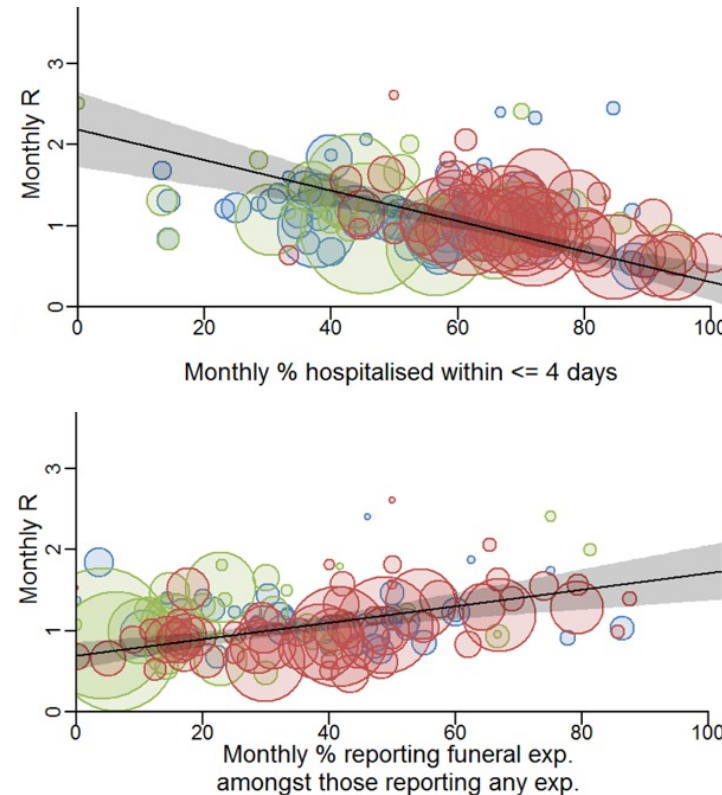
It can still allow exploring the impact of interventions (albeit in a simple way)



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

(as long as you record information about interventions...)



WHO Ebola Response Team PLoS Med 2016
Cori et al. Phil Transac Roy Soc B 2017

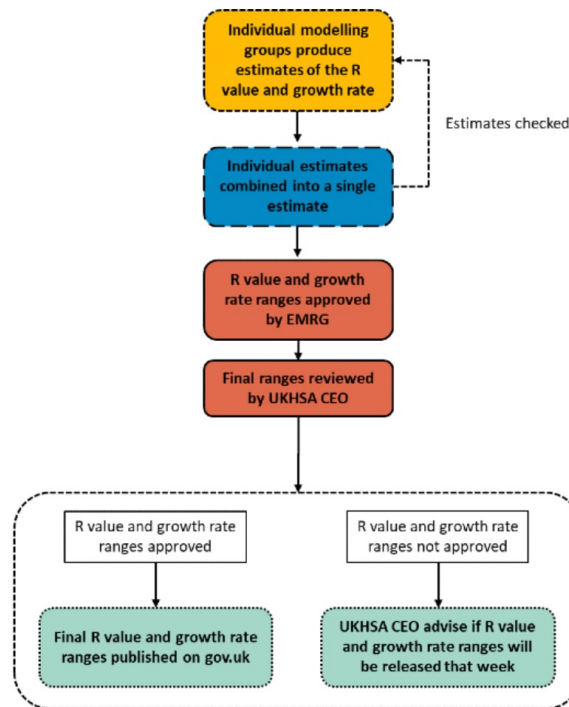
It is perhaps best used in combination with other more complex models?



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

Flowchart: estimating the R value and growth rate – from production to publication



More complex models take time to develop, and may be the first to be dropped as we get out of the most acute phase

→ useful to have simpler model informing pooled estimates



MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

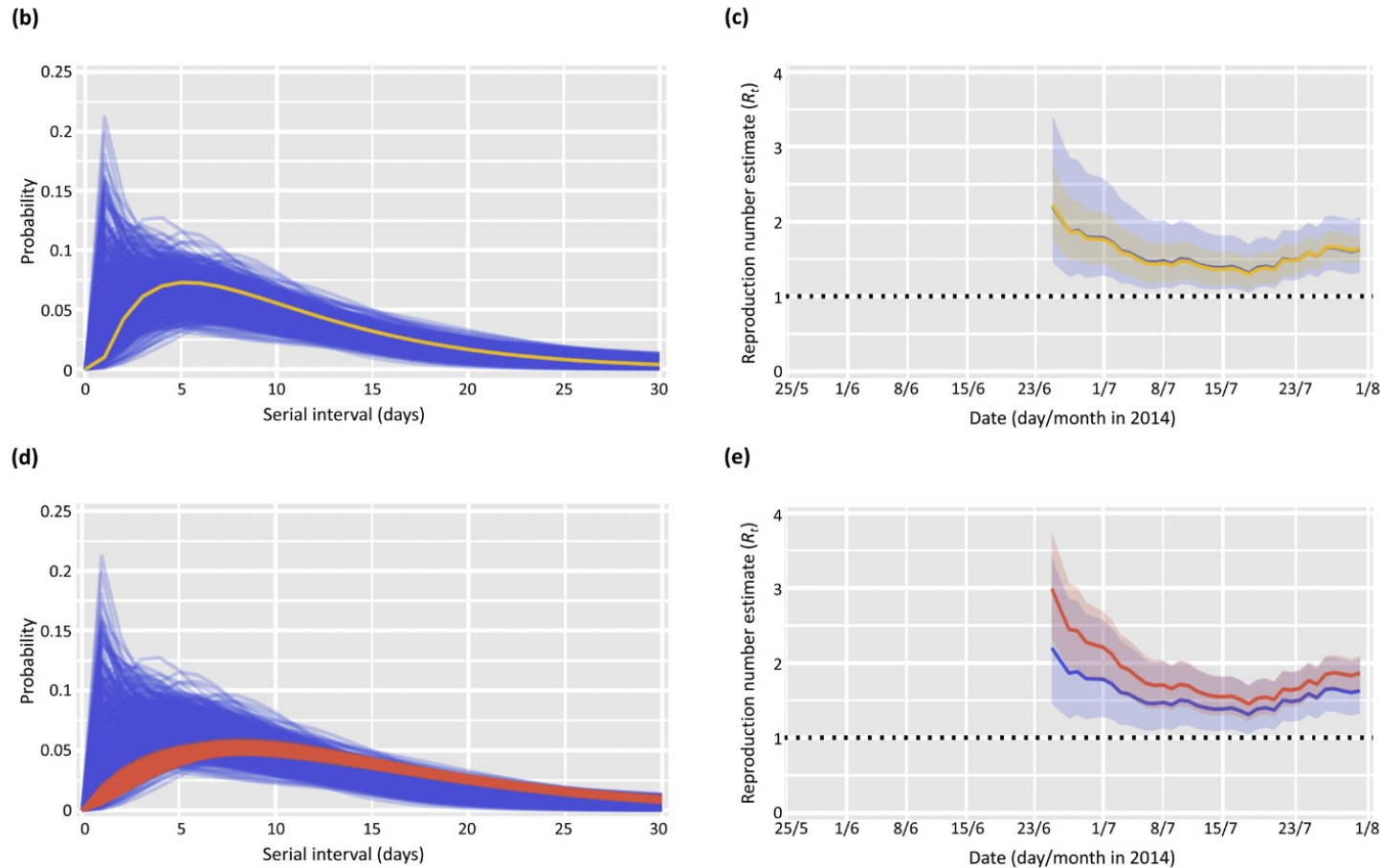
Benefits of it being so simple:
We can add features pretty easily
whilst keeping the model and software relatively simple

Using the latest data informing the serial interval



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London



→ Can make a large difference in the R estimates

Fig. 4. Estimates of the time-dependent reproduction number, R_t , for the early part of the 2013–2016 Ebola outbreak in Liberia (International Ebola Response Team,

Thompson et al. *Epidemics* 2019

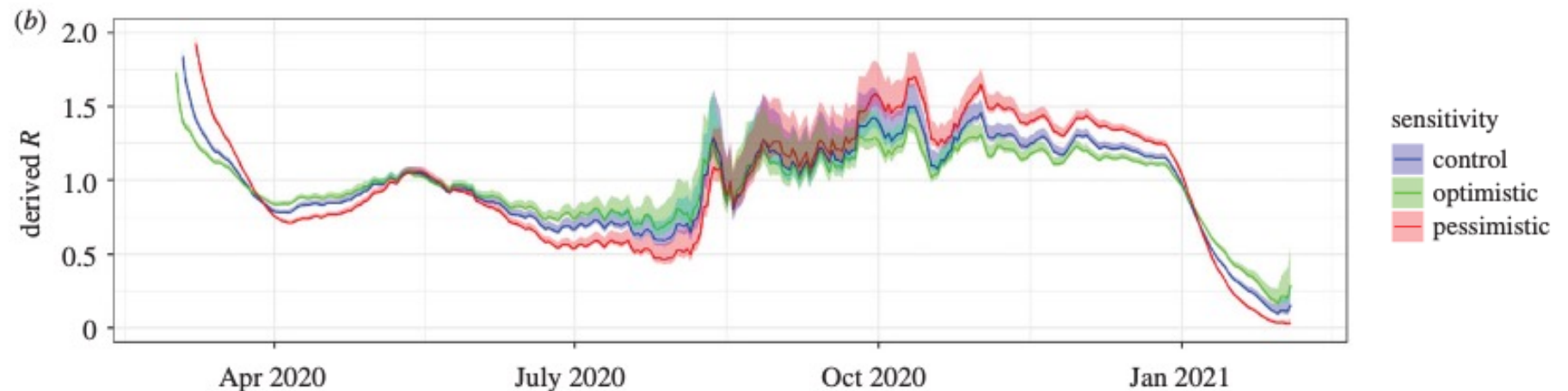
Accounting for heterogeneities in the serial interval



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

- Using a single type branching process can lead to biases in R estimates
- Bias is small for isolating / non isolating, but can be large for symptomatic / asymptomatic, vaccinated / unvaccinated if those have different serial intervals



- Importance of characterising the serial interval of an “average” transmission pair, not just from symptomatic unvaccinated cases.

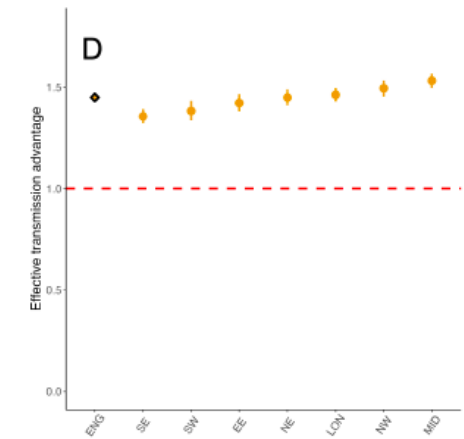
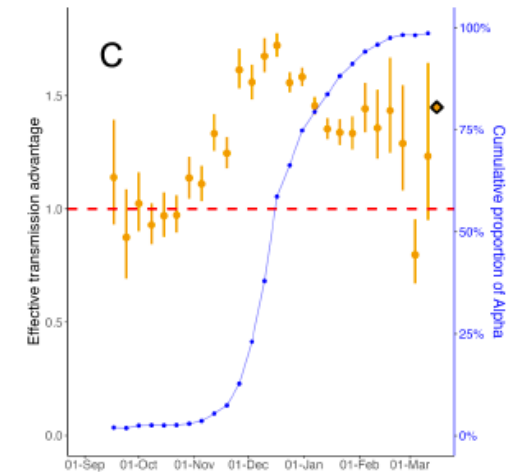
Estimating the transmission advantage of novel variants / strains



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

- Extending EpiEstim (analytically tractable marginal posteriors)
 - Fast, so can
 - explore spatiotemporal heterogeneity
 - pool information where relevant
- Retrospective analysis of the Alpha variant,
- prospective analysis for Delta & Omicron
- Measures the “effective transmission advantage”
 - First step in quantifying threat from new variants



Estimating R from data reported over long time intervals



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

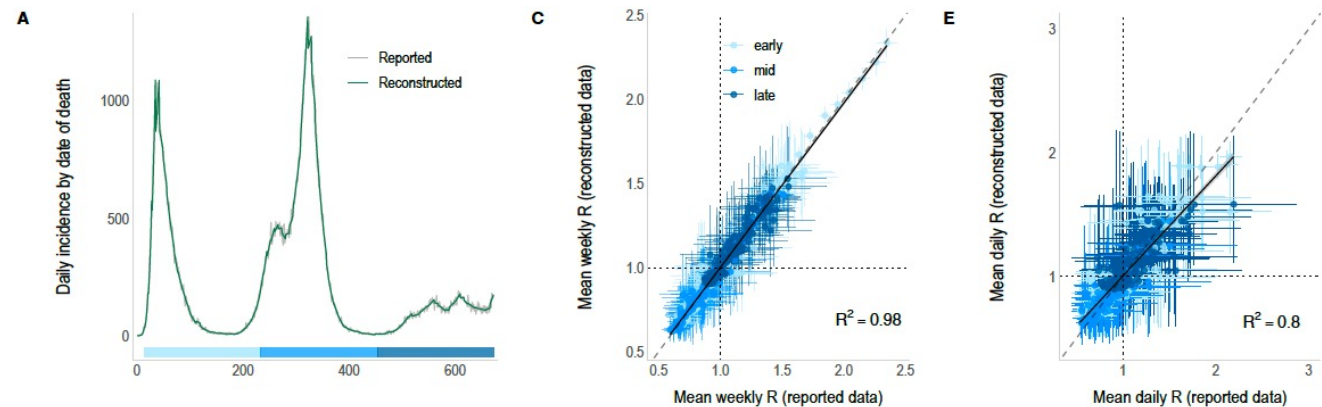
- Expectation-Maximisation algorithm combined with EpiEstim to reconstruct daily incidence and estimate R
- Applied to COVID and flu daily data which we aggregated

→ Expands applicability of EpiEstim (e.g. for less acute COVID phase)

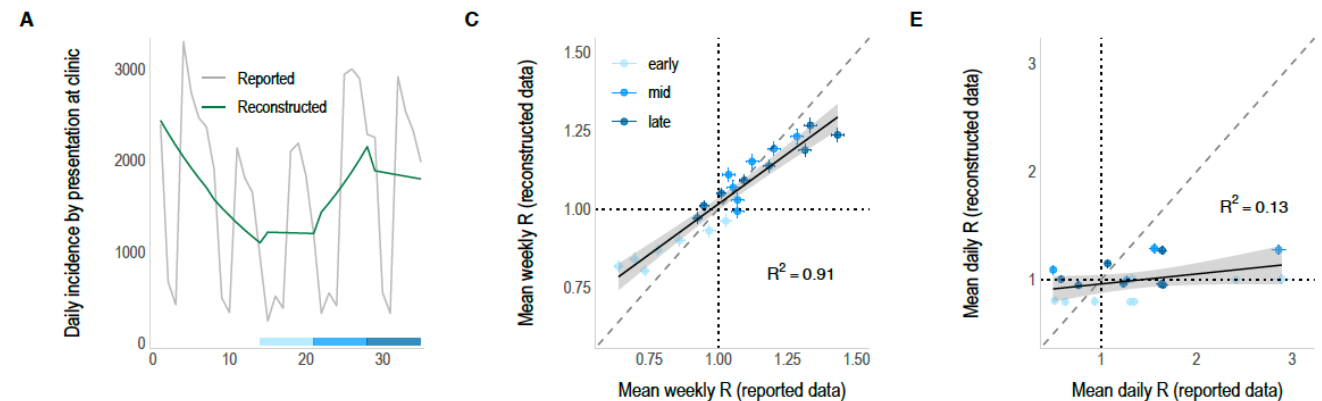
→ May be useful even when data is reported daily but with administrative noise

Nash et al. in prep

COVID-19 deaths in the UK



ILI in US military (2009-10)





MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

**What context has EpiEstim been applied to,
and what features have others been adding?**

What are people using this for?



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

• Literature review + survey of EpiEstim users

Disease/disease agent investigated	<i>n</i>
COVID-19	198
Ebola Virus Disease (EVD)	7
Influenza	7
Measles	4
Multiple diseases	3
Cholera	3
Zika	2
Severe Acute Respiratory Syndrome (SARS)	2
Respiratory Syncytial Virus (RSV)	2
Middle East Respiratory Syndrome (MERS)	2
Other	12

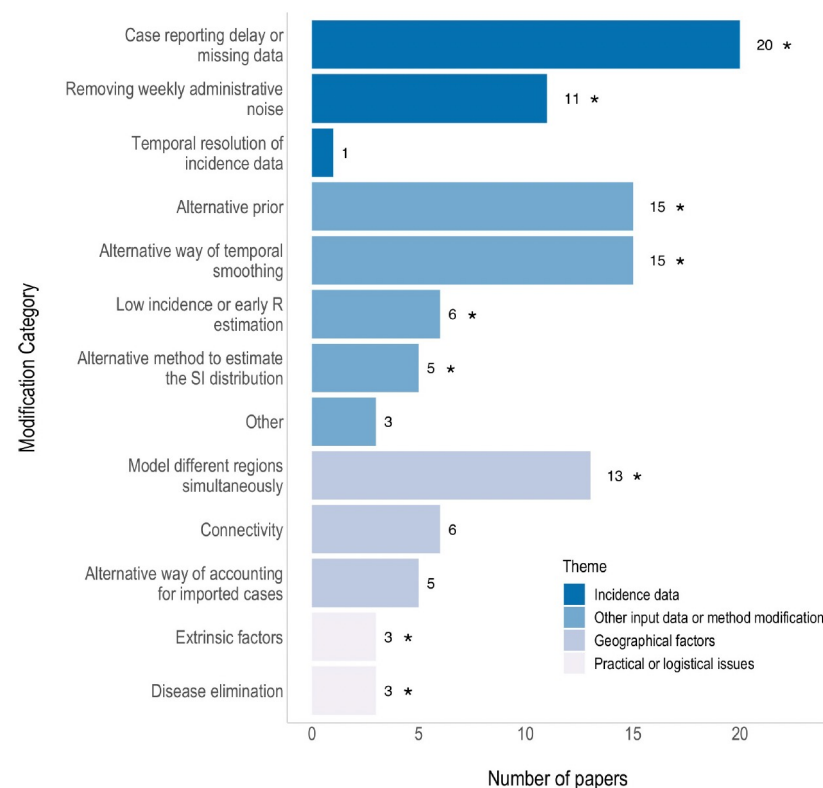


Fig 3. Summary of the modifications made to the EpiEstim method in 54 papers. Papers which made multiple modifications are counted more than once. Asterisks are present next to the modification category if an R package or opensource tool has been identified that addresses an issue within that category. See text for a description of all modifications and [Table 2](#) for a summary of the R packages identified.

Review of software



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

Table 2. Summary table of the R packages and tool (*) that address some of the issues identified in the scoping review. The ticks (✓) indicate whether an R package includes that modification type and rows with hash lines show the modification types that have not been incorporated into a known R package or tool. The final three rows summarise additional exploration by the authors to assess how easily each package/tool can be installed and used. For full details of how each classification (very good = ✓✓, good = ✓, poor = ✗) was defined, see Table B in [S1 Text](#) and the associated text (section 3).

Theme	Modification type	APEestim (v 0.0.1)	bayEStim (v 0.0.1)	earlyR (v 0.0.5)	epicontacts (v 1.1.2)	Epidemia (v 1.0.0)	EpiFilter* (* Tool)	EpiNow2 (v 1.3.2)
Incidence	Case reporting delay or missing data		✓			✓		✓
	Removing weekly administrative noise							✓
	Temporal resolution of incidence data							
Other input data or method modification	Low incidence or early R estimation			✓			✓	
	Alternative prior					✓	✓	✓
	Alternative way of temporal smoothing	✓				✓	✓	✓
	Alternative method to estimate the SI distribution				✓			
Geographical factors	Connectivity							
	Model different regions simultaneously					✓		✓
	Alternative way of accounting for imported cases							
Practical/logistical	Extrinsic factors					✓		
	Disease elimination						✓	
Additional exploration (✓✓ = very good, ✓ = good, ✗ = poor)								
Usability	Ease of installation	✓	✗	✓✓	✓✓	✗	✗	✓
	Documentation and tutorials (e.g., vignette)	✗	✗	✓✓	✓✓	✓✓	✓✓	✓✓
	Speed of R estimation [◇] (◇ except for epicontacts, which estimates the SI)	✓✓	NA	✓✓	✓✓ [◇]	✓	✓✓	✗

An epidemic of methods / software?



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

-
- With homoplasy?!
 - Many methods are not implemented in easily useable ready to use software
 - Little systematic comparison of performance / clarity on when one should use which software

Ongoing work and future priorities

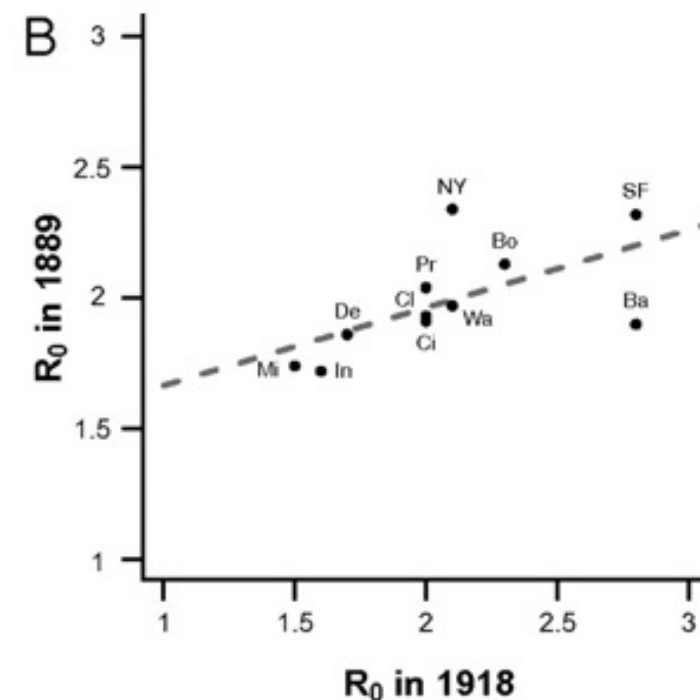


MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

- Strategy for method and software development? Discussion welcome!
- Comparison of methods + understanding what is “worth” the effort, in what context:
 - Changes in the serial interval over time
 - Super-spreading
 - Ideal temporal and spatial scale of analysis?
- Implications for forecasting
- Retrospective analyses can involve simple models to test hypotheses, e.g. locations at risk?

Valleron et al. PNAS 2010



Conclusion



MRC Centre for
Global Infectious
Disease Analysis

Imperial College
London

-
- Simple ready-to-use tools are important for rapid outbreak assessment
 - estimation of R but many other epidemic characteristics
 - Most countries do not have SPI-M
 - with tens of groups contributing weekly situation updates based on complex modelling
 - Even in countries who do, having simple ready-to-use tools is critical
 - in the early days
 - as a benchmark
 - Tools are only useful if they are useable in practice
 - R is important but doesn't tell you the whole picture

Acknowledgements



MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

Imperial College London

- Sangeeta Bhatia, Neil Ferguson, Will Green, Rebecca Nash, Jack Wardle
- The Imperial College real time COVID-19 modelling team

University of Sussex

Pierre Nouvellet

University of Oxford

Christophe Fraser

Institut Pasteur

Simon Cauchemez

University of Warwick

Robin Thompson

EpiEstim contributors and users

Funders:

MRC, NIHR HPRU



MRC Centre for
Global Infectious
Disease Analysis

**Imperial College
London**

Questions?