

# **Complex Fluids with Mobile Charge-Regulated Macro-Ions**





### What is Charge Regulation?

Modeling of *soft* immobile surfaces - boundary condition of the **Poisson-Boltzmann equation:** 

- Law of mass action (le Chatelier's principle)
- $F = F_{PR} + g_{S}$ Free-energy formulation ×.

### Is Charge-Regulation a generalized b.c.?









#### Markovich, Andelman and Podgornik, EPL, 2016



# Complex Fluids with Mobile Charge-Regulated Macro-Ions



**BLAVATNIK** FAMILY FOUNDATION

Relevant to solution of proteins with dissociable amino acids or charged nano-particles with dissociable surface groups

- Mobile ions and macro-ions in solution
- Charge-Regulation is no longer a fixed boundary condition!
- Macro-ions are taken as point-like -- ideal gas entropy

$$F = F_{\rm PB} + g(\phi, \psi) + [p \ln(pa^3) - p] - \mu_p p$$



$$g(\phi, \psi) = \lim_{a \to 0} \frac{1}{4\pi a^2} \oint_{r'=a} d^2 r' g_S(\phi(r'), \psi(r'))$$



modified double-layer structure



buffering



Markovich, Andelman and Podgornik, submitted, 2017